4. Parsing in Practice

Oscar Nierstrasz

Thanks to Jens Palsberg and Tony Hosking for their kind permission to reuse and adapt the CS132 and CS502 lecture notes.
http://www.cs.ucla.edu/~palsberg/
http://www.cs.purdue.edu/homes/hosking/
Roadmap

> Bottom-up parsing
> LR(k) grammars
> JavaCC, Java Tree Builder and the Visitor pattern
> Example: a straightline interpreter

See, Modern compiler implementation in Java (Second edition), chapters 3-4.
Roadmap

- Bottom-up parsing
- LR(k) grammars
- JavaCC, Java Tree Builder and the Visitor pattern
- Example: a straightline interpreter
Some definitions

*Recall:*

> For a grammar $G$, with start symbol $S$, any string $\alpha$ such that $S \Rightarrow^* \alpha$ is called a [sentential form](#).

— If $\alpha \in V_t^*$, then $\alpha$ is called a [sentence](#) in $L(G)$
— Otherwise it is just a sentential form (not a sentence in $L(G)$)

> A [left-sentential form](#) is a sentential form that occurs in the leftmost derivation of some sentence.

> A [right-sentential form](#) is a sentential form that occurs in the rightmost derivation of some sentence.
Bottom-up parsing

**Goal:**
—Given an input string $w$ and a grammar $G$, construct a parse tree by starting at the leaves and working to the root.

> The parser repeatedly matches a *right-sentential form* from the language against the tree’s upper frontier.
> At each match, it applies a *reduction* to build on the frontier:
  —each reduction matches an upper frontier of the partially built tree to the RHS of some production
  —each reduction adds a node on top of the frontier
> The final result is a *rightmost derivation*, in reverse.

Why rightmost?
Example

Consider the grammar:

1. \( S \to aABe \)
2. \( A \to Abc \)
3. \( | \to b \)
4. \( B \to d \)

and the input string: \( abbcde \)

Parse bottom up, replacing terms by non-terminals.
Reading in reverse, we have a rightmost derivation, first replacing \( S \), then \( B \), \( A \) and \( A \) again.
Note that you have more context than with top-down since you may have a whole AST on the stack (A)
A handle of a right-sentential form $\gamma$ is a production $A \rightarrow \beta$ and a position in $\gamma$ where $\beta$ may be found and replaced by $A$ to produce the previous right-sentential form in a rightmost derivation of $\gamma$.

Suppose: $S \Rightarrow^* \alpha Aw \Rightarrow \alpha \beta w$.
Then $A \rightarrow \beta$ in the position following $\alpha$ is a handle of $\alpha \beta w$.

NB: Because $\gamma$ is a right-sentential form, the substring to the right of a handle contains only terminal symbols.

Non-terminals are only to the left (the stack) since you are parsing left-to-right.
The handles in our previous example correspond to the points where we prune (reduce).
**Theorem:**

If $G$ is unambiguous then every right-sentential form has a unique handle.

**Proof:** (by definition)

1. $G$ is unambiguous $\Rightarrow$ rightmost derivation is unique
2. $\Rightarrow$ a unique production $A \rightarrow \beta$ applied to take $\gamma_{i-1}$ to $\gamma_i$
3. $\Rightarrow$ a unique position $k$ at which $A \rightarrow \beta$ is applied
4. $\Rightarrow$ a unique handle $A \rightarrow \beta$
The left-recursive expression grammar (*original form*)

1. `<goal>` ::= `<expr>`
2. `<expr>` ::= `<expr>` + `<term>`
3. | `<expr>` - `<term>`
4. | `<term>`
5. `<term>` ::= `<term>` * `<factor>`
6. | `<term>` / `<factor>`
7. | `<factor>`
8. `<factor>` ::= num
9. | id

How do we parse (bottom-up) to arrive at this derivation?

Once again, lookahead tells us to reduce `<term>*<factor>` and not `<expr>—<term>`
The question is, how do we arrive at this derivation?
The process to construct a bottom-up parse is called **handle-pruning**.

To construct a rightmost derivation

\[ S = Y_0 \Rightarrow Y_1 \Rightarrow Y_2 \Rightarrow \ldots \Rightarrow Y_{n-1} \Rightarrow Y_n = w \]

we set \( i \) to \( n \) and apply the following simple algorithm:

For \( i = n \) down to 1

1. Find the handle \( A_i \rightarrow \beta_i \) in \( Y_i \)
2. Replace \( \beta_i \) with \( A_i \) to generate \( Y_{i-1} \)

**This takes 2n steps, where \( n \) is the length of the derivation**
### Stack implementation

> One scheme to implement a handle-pruning, bottom-up parser is called a **shift-reduce parser**.

> Shift-reduce parsers use a **stack** and an **input buffer**

1. Initialize stack with `$`
2. Repeat until the top of the stack is the goal symbol and the input token is `$`
   a) **Find the handle.**
      *If we don’t have a handle on top of the stack, shift (push) an input symbol onto the stack*
   b) **Prune the handle.**
      *If we have a handle $A \rightarrow \beta$ on the stack, reduce*
      i. Pop $|\beta|$ symbols off the stack
      ii. Push $A$ onto the stack

**NB:** In practice we also lookahead to determine whether to shift or reduce!

Actually, this is an LR(0) parser algorithm, since no lookahead is used.
1. Shift until top of stack is the right end of a handle
2. Find the left end of the handle and reduce

Why does \texttt{<expr>-<term>} produce a shift rather than a reduce? Actually we need to lookahead at least one character (LR(1)) to decide whether to shift or reduce.
### Shift-reduce parsing

A shift-reduce parser has just four canonical actions:

<table>
<thead>
<tr>
<th>Action</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>shift</strong></td>
<td>next input symbol is shifted (pushed) onto the top of the stack</td>
</tr>
<tr>
<td><strong>reduce</strong></td>
<td>right end of handle is on top of stack; locate left end of handle within the stack; pop handle off stack and push appropriate non-terminal LHS</td>
</tr>
<tr>
<td><strong>accept</strong></td>
<td>terminate parsing and signal success</td>
</tr>
<tr>
<td><strong>error</strong></td>
<td>call an error recovery routine</td>
</tr>
</tbody>
</table>

*The key problem: to recognize handles (not covered in this course).*

Ugh! Where is this covered?
Roadmap

- Bottom-up parsing
- LR(k) grammars
- JavaCC, Java Tree Builder and the Visitor pattern
- Example: a straightline interpreter
LR(k) grammars

A grammar G is LR(k) iff:

1. \[ S \Rightarrow_{rm}^* \alpha Aw \Rightarrow_{rm} \alpha \beta w \]
2. \[ S \Rightarrow_{rm}^* \gamma Bx \Rightarrow_{rm} \alpha \beta y \]
3. \[ \text{FIRST}_k(w) = \text{FIRST}_k(y) \Rightarrow \alpha Ay = \gamma Bx \]

I.e., if \( \alpha \beta w \) and \( \alpha \beta y \) have the same k-symbol lookahead, then there is a unique handle to reduce in the rightmost derivation.

Assume sentential forms \( \alpha \beta w \) and \( \alpha \beta y \), with common prefix \( \alpha \beta \) and common k-symbol lookahead \( \text{FIRST}_k(w) = \text{FIRST}_k(y) \), such that \( \alpha \beta w \) reduces to \( \alpha Aw \) and \( \alpha \beta y \) reduces to \( \gamma Bx \).
But, the common prefix means \( \alpha \beta y \) also reduces to \( \alpha Ay \), for the same result.
Thus \( \alpha Ay = \gamma Bx \)
Why study LR grammars?

**LR(1) grammars are used to construct LR(1) parsers.**

— everyone’s favorite parser
— virtually all context-free programming language constructs can be expressed in an LR(1) form
— LR grammars are the most general grammars parsable by a deterministic, bottom-up parser
— efficient parsers can be implemented for LR(1) grammars
— LR parsers detect an error as soon as possible in a left-to-right scan of the input
— LR grammars describe a proper superset of the languages recognized by predictive (i.e., LL) parsers

**LL(k):** recognize use of a production $A \rightarrow \beta$ seeing first $k$ symbols of $\beta$

**LR(k):** recognize occurrence of $\beta$ (the handle) having seen all of what is derived from $\beta$ plus $k$ symbols of look-ahead

Recall: LL(k) is top-down, LR(k) is bottom-up.
# Left versus right recursion

> **Right Recursion:**
> — needed for termination in predictive parsers
> — requires more stack space
> — right associative operators

> **Left Recursion:**
> — works fine in bottom-up parsers
> — limits required stack space
> — left associative operators

> **Rule of thumb:**
> — right recursion for *top-down parsers*
> — left recursion for *bottom-up parsers*
> **Recursive descent**
  — A hand coded recursive descent parser directly encodes a grammar (typically an LL(1) grammar) into a series of mutually recursive procedures. It has most of the linguistic limitations of LL(1).

> **LL(k):**
  — must be able to recognize the use of a production after seeing only the first k symbols of its right hand side.

> **LR(k):**
  — must be able to recognize the occurrence of the right hand side of a production after having seen all that is derived from that right hand side with k symbols of look-ahead.

> **The dilemmas:**
  — LL dilemma: pick $A \rightarrow b$ or $A \rightarrow c$ ?
  — LR dilemma: pick $A \rightarrow b$ or $B \rightarrow b$ ?
Roadmap

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The Java Compiler Compiler

- "Lex and Yacc for Java."
- Based on **LL(k)** rather than LR(1) or LALR(1).
- Grammars are written in EBNF.
- Transforms an EBNF grammar into an LL(k) parser.
- Supports embedded action code written in Java (just like Yacc supports embedded C action code)
- The look-ahead can be changed by writing `LOOKAHEAD(…)`
- The whole input is given in just one file (not two).

LALR parsers start with an LR(0) state machine and then compute lookahead *sets* for all rules in the grammar, checking for ambiguity.
The JavaCC input format

> Single file:
  — header
  — token specifications for lexical analysis
  — grammar
Examples

Token specification:

```
TOKEN : /* LITERALS */
{
  < INTEGER_LITERAL: ( ["1"-"9"] ("0"-"9")* | "0") >
}
```

Production:

```
Declarations

void StmList() : 
{

Productions and actions

  Stm() ( ";" Stm() ) *

}
```

NB: with Java Tree Builder, the actual declarations and actions are inferred and generated.
Generating a parser with JavaCC

javacc fortran.jj  // generates a parser
javac Main.java   // Main.java calls the parser
java Main < prog.f // parses the program prog.f

NB: JavaCC is just one of many tools available ...
See: http://catalog.compilertools.net/java.html
The Visitor Pattern

> Intent:
—Represent an operation to be performed on the elements of an object structure. Visitor lets you define a new operation without changing the classes of the elements on which it operates.
> When using the Visitor pattern,
   —the set of classes must be fixed in advance, and
   —each class must have an `accept` method.
First Approach: `instanceof` and downcasts

The running Java example: summing an integer list.

```java
public interface List {}
public class Nil implements List {
    int head;
    List tail;
    Cons(int head, List tail) {
        this.head = head;
        this.tail = tail;
    }
}

public class Cons implements List {
    int head;
    List tail;
    Cons(int head, List tail) {
        this.head = head;
        this.tail = tail;
    }
}

public class SumList {
    public static void main(String[] args) {
        List l = new Cons(5, new Cons(4, new Cons(3, new Nil())));
        int sum = 0;
        boolean proceed = true;
        while (proceed) {
            if (l instanceof Nil) {
                proceed = false;
            } else if (l instanceof Cons) {
                sum = sum + ((Cons) l).head;
                l = ((Cons) l).tail;
            }
        }
        System.out.println("Sum = " + sum);
    }
}
```

**Advantage:** The code does not touch the classes Nil and Cons.

**Drawback:** The code must use downcasts and `instanceof` to check what kind of List object it has.
Second Approach: Dedicated Methods

The classical OO approach is to offer dedicated methods through a common interface.

```
public interface List {
    public int sum();
}

public class Nil implements List {
    public int sum() {
        return 0;
    }
}

public class Cons implements List {
    int head;
    List tail;
    Cons(int head, List tail) {
        this.head = head;
        this.tail = tail;
    }
    public int sum() {
        return head + tail.sum();
    }
}

public class SumList {
    public static void main(String[] args) {
        List l = new Cons(5, new Cons(4,
                new Cons(3, new Nil())));
        System.out.println("Sum = "+ l.sum());
    }
}
```

**Advantage:** Downcasts and instanceof calls are gone, and the code can be written in a systematic way.

**Disadvantage:** For each new operation on List-objects, new dedicated methods have to be written, and all classes must be recompiled.
Third Approach: The Visitor Pattern

> The Idea:
  — Divide the code into an object structure and a Visitor
  — Insert an accept method in each class. Each accept method takes a Visitor as argument.
  — A Visitor contains a visit method for each class (overloading!). A method for a class C takes an argument of type C.

NB: In a dynamically typed language you would introduce a visitC method for each class C.
Third Approach: The Visitor Pattern

```java
public interface List {
    public void accept(Visitor v);
}
public class Nil implements List {
    public void accept(Visitor v) {
        v.visit(this);
    }
}
public class Cons implements List {
    int head;
    List tail;
    Cons(int head, List tail) {… }
    public void accept(Visitor v) {
        v.visit(this);
    }
}
public interface Visitor {
    void visit(Nil l);
    void visit(Cons l);
}
```

```java
public class SumVisitor implements Visitor {
    int sum = 0;
    public void visit(Nil l) { }
    public void visit(Cons l) {
        sum = sum + l.head;
        l.tail.accept(this);
    }
}
```

```java
public static void main(String[] args) {
    List l = new Cons(5, new Cons(4,
        new Cons(3, new Nil())));
    l.accept(sv);
    System.out.println("Sum = " + sv.sum);
}
```

**NB:** The visit methods capture both (1) actions, and (2) access of subobjects.

Note how in Java the type system is used to disambiguate the different visit() methods. In a dynamic language, there would be visitNil() and visitCons() methods.
**Comparison**

The Visitor pattern combines the advantages of the two other approaches.

<table>
<thead>
<tr>
<th></th>
<th>Frequent downcasts?</th>
<th>Frequent reccompilation?</th>
</tr>
</thead>
<tbody>
<tr>
<td>instanceof + downcasting</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>dedicated methods</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Visitor pattern</td>
<td>No</td>
<td>No</td>
</tr>
</tbody>
</table>

JJTree (Sun) and Java Tree Builder (Purdue/UCLA) are front-ends for JavaCC that are based on Visitors.
**Visitors: Summary**

- A visitor gathers related operations.
  - It also separates unrelated ones.
  - Visitors can accumulate state.
- Visitor makes adding new operations easy.
  - Simply write a new visitor.
- Adding new classes to the object structure is hard.
  - Key consideration: are you most likely to change the algorithm applied over an object structure, or are you most likely to change the classes of objects that make up the structure?
- Visitor can break encapsulation.
  - Visitor’s approach assumes that the interface of the data structure classes is powerful enough to let visitors do their job. As a result, the pattern often forces you to provide public operations that access internal state, which may compromise its encapsulation.
The Java Tree Builder (JTB)

- front-end for The Java Compiler Compiler.
- supports the building of syntax trees which can be traversed using visitors.
- transforms a bare JavaCC grammar into three components:
  - a JavaCC grammar with embedded Java code for building a syntax tree;
  - one class for every form of syntax tree node; and
  - a default visitor which can do a depth-first traversal of a syntax tree.

http://compilers.cs.ucla.edu/jtb/
The produced JavaCC grammar can then be processed by the Java Compiler Compiler to give a parser which produces syntax trees. The produced syntax trees can now be traversed by a Java program by writing subclasses of the default visitor.
Using JTB

```
jtb fortran.jj     // generates jtb.out.jj
javacc jtb.out.jj   // generates a parser
javac Main.java    // Main.java calls the parser and visitors
java Main < prog.f // builds a syntax tree and executes visitors
```
Roadmap

> Bottom-up parsing
> LR(k) grammars
> JavaCC, Java Tree Builder and the Visitor pattern
> **Example: a straightline interpreter**
Recall our straight-line grammar

<table>
<thead>
<tr>
<th>Non-terminal</th>
<th>Production</th>
<th>Non-terminal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stm</td>
<td>→ Stm ; Stm</td>
<td>CompoundStm</td>
</tr>
<tr>
<td>Stm</td>
<td>→ id := Exp</td>
<td>AssignStm</td>
</tr>
<tr>
<td>Stm</td>
<td>→ print ( ExpList )</td>
<td>PrintStm</td>
</tr>
<tr>
<td>Exp</td>
<td>→ id</td>
<td>IdExp</td>
</tr>
<tr>
<td>Exp</td>
<td>→ num</td>
<td>NumExp</td>
</tr>
<tr>
<td>Exp</td>
<td>→ Exp Binop Exp</td>
<td>OpExp</td>
</tr>
<tr>
<td>Exp</td>
<td>→ ( Stm, Exp )</td>
<td>EseqExp</td>
</tr>
<tr>
<td>ExpList</td>
<td>→ Exp , ExpList</td>
<td>PairExpList</td>
</tr>
<tr>
<td>ExpList</td>
<td>→ Exp</td>
<td>LastExpList</td>
</tr>
<tr>
<td>Binop</td>
<td>→ +</td>
<td>Plus</td>
</tr>
<tr>
<td>Binop</td>
<td>→ −</td>
<td>Minus</td>
</tr>
<tr>
<td>Binop</td>
<td>→ ×</td>
<td>Times</td>
</tr>
<tr>
<td>Binop</td>
<td>→ /</td>
<td>Div</td>
</tr>
</tbody>
</table>
Straightline Interpreter Files

Source files

- «Grammar spec»
  - slpl.jj

- «Default visitors and interfaces»
  - Visitor ...

- «Interpreter source»
  - InterpreterVisitor ...

- «Abstract Machine for Interpreter»
  - Machine

Generated files

- «Grammar spec with actions»
  - jtb.out.jj

- «Parser source»
  - StraightLineParser ...

- «Syntax Tree Nodes»
  - Goal ...

- «Bytecode»
  - StraightLineParser ...

JavaCC generates Key JTB visits Source files

- JavaCC

produces

Key generates

38
Tokens

slp1.jj starts with the
scanner declarations

```java
options {
    JAVA_UNICODE_ESCAPE = true;
}

PARSER_BEGIN(StraightLineParser)
package parser;
public class StraightLineParser {
PARSER_END(StraightLineParser)

SKIP : /* WHITE SPACE */
{ " " | \t | \n | \r | \f }

TOKEN :
{ < SEMICOLON: ; >
| < ASSIGN: := >
| ...
}

TOKEN : /* LITERALS */
{ < INTEGER_LITERAL: ([\d]-[\d]* \[0-9\]*)* \0 >
}

TOKEN : /* IDENTIFIERS */
{ < IDENTIFIER: <LETTER> (<LETTER>|<DIGIT>)* >
| < #LETTER: [a-zA-Z] >
| < #DIGIT: [0-9] >
}
```
Rewriting our grammar

<table>
<thead>
<tr>
<th>Rule</th>
<th>Productions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Goal</td>
<td>$\rightarrow$ StmList</td>
</tr>
<tr>
<td>StmList</td>
<td>$\rightarrow$ Stm ( ; Stm ) *</td>
</tr>
<tr>
<td>Stm</td>
<td>$\rightarrow$ id := Exp</td>
</tr>
<tr>
<td></td>
<td>$\mid$ print (&quot; ExpList &quot;)</td>
</tr>
<tr>
<td>Exp</td>
<td>$\rightarrow$ MulExp (( +</td>
</tr>
<tr>
<td>MulExp</td>
<td>$\rightarrow$ PrimExp ((*</td>
</tr>
<tr>
<td>PrimExp</td>
<td>$\rightarrow$ id</td>
</tr>
<tr>
<td></td>
<td>$\mid$ num</td>
</tr>
<tr>
<td></td>
<td>$\mid$ (&quot; StmList , Exp &quot;)</td>
</tr>
<tr>
<td>ExpList</td>
<td>$\rightarrow$ Exp ( , Exp ) *</td>
</tr>
</tbody>
</table>

We introduce a start rule, eliminate all left-recursion, and establish precedence.
Grammar rules

The grammar rules directly reflect our BNF!

NB: We add some non-terminals to help our visitors.

```c
void Goal() : {} { StmList() <EOF> }
void StmList() : {}{ Stm() ( ;" Stm() ) * }
void Stm() : {} { Assignment() | PrintStm() }

/* distinguish reading and writing Id */
void Assignment() : {} { WriteId() ":=" Exp() }
void WriteId() : {} { <IDENTIFIER> }

void PrintStm() : {} { "print" (" ExpList() ")" }
void ExpList() : {} { Exp() ( AppendExp() ) * }
void AppendExp() : {} { "," Exp() }

void Exp() : {} { MulExp() ( PlusOp() | MinOp() ) * }
void PlusOp() : {} { "+" MulExp() }
void MinOp() : {} { "-" MulExp() }

void MulExp() : {} { PrimExp() ( MulOp() | DivOp() ) * }
void MulOp() : {} { "*" PrimExp() }
void DivOp() : {} { "/" PrimExp() }

void PrimExp() : {}{ ReadId() | Num() | StmExp() }
void ReadId() : {}{ <IDENTIFIER> }
void Num() : {}{ <INTEGER_LITERAL> }
void StmExp() : {}{ (" StmList() "," Exp() ")" }
```

Java Tree Builder

JTB automatically generates actions to build the syntax tree, and visitors to visit it.

---

```java
// Generated by JTB 1.3.2
options {
  JAVA_UNICODE_ESCAPE = true;
}
PARSER_BEGIN(StraightLineParser)
package parser;
import syntaxtree.*;
import java.util.Vector;

public class StraightLineParser {
  
  Goal Goal() {
    StmList n0;
    NodeToken n1;
    Token n2;
  }
  { n0=StmList();
    n2=<EOF> { 
      n2.beginColumn++; n2.endColumn++;
      n1 = JTBToolkit.makeNodeToken(n2);
    }
    { return new Goal(n0,n1); } 
  }
} ...
```
Straightline Interpreter Runtime

- «Straightline source code»
- Examples
  - StraightLineParser
  - «Syntax Tree»
      - Goal ...
  - visit
  - InterpreterVisitor ...
      - instructs
  - Machine
  - output

- Key
  - generates
The interpreter

package interpreter;
import ...;
public class StraightLineInterpreter {
    Goal parse;
    StraightLineParser parser;

    public static void main(String[] args) {
        System.out.println(new StraightLineInterpreter(System.in).interpret());
    }

    public StraightLineInterpreter(InputStream in) {
        parser = new StraightLineParser(in);
        this.initParse();
    }

    private void initParse() {
        try { parse = parser.Goal(); } catch (ParseException e) { ... }
    }

    public String interpret() {
        assert(parse != null);
        Visitor visitor = new Visitor();
        visitor.visit(parse);
        return visitor.result();
    }
}

The interpreter simply runs the parser and visits the parse tree.
An abstract machine for straight line code

```java
package interpreter;
import java.util.*;
public class Machine {
    private Hashtable<String,Integer> store; // current values of variables
    private StringBuffer output; // print stream so far
    private int value; // result of current expression
    private Vector<Integer> vlist; // list of expressions computed

    public Machine() {
        store = new Hashtable<String,Integer>();
        output = new StringBuffer();
        setValue(0);
        vlist = new Vector<Integer>();
    }

    void assignValue(String id) { store.put(id, getValue()); }
    void appendExp() { vlist.add(getValue()); }
    void printValues() {...}
    void setValue(int value) {...}
    int getValue() { return value; }

    void readValueFromId(String id) {
        assert isDefined(id); // precondition
        this.setValue(store.get(id));
    }

    private boolean isDefined(String id) { return store.containsKey(id); }
    String result() { return this.output.toString(); }
}
```

The Visitor interacts with this machine as it visits nodes of the program.
The visitor

```java
package interpreter;
import visitor.DepthFirstVisitor;
import syntaxtree.*;

public class Visitor extends DepthFirstVisitor {
    Machine machine;
    public Visitor() { machine = new Machine(); }
    public String result() { return machine.result(); }

    public void visit(Assignment n) {
        n.f0.accept(this);
        n.f1.accept(this);
        n.f2.accept(this);
        String id = n.f0.f0.tokenImage;
        machine.assignValue(id);
    }

    public void visit(PrintStm n) { ... }
    public void visit(AppendExp n) { ... }
    public void visit(PlusOp n) { ... }
    public void visit(MinOp n) { ... }
    public void visit(MulOp n) { ... }
    public void visit(DivOp n) { ... }
    public void visit(ReadId n) { ... }
    public void visit(Num n) { ... }
}
```

The Visitor interprets interesting nodes by directly interacting with the abstract machine.
What you should know!

✎ Why do bottom-up parsers yield rightmost derivations?
✎ What is a “handle”? How is it used?
✎ What is “handle-pruning”? How does a shift-reduce parser work?
✎ When is a grammar LR(k)?
✎ Which is better for hand-coded parsers, LL(1) or LR(1)?
✎ What kind of parsers does JavaCC generate?
✎ How does the Visitor pattern help you to implement parsers?
Can you answer these questions?

- What are “shift-reduce” errors?
- How do you eliminate them?
- Which is more expressive? LL(k) or LR(k)?
- How would you implement the Visitor pattern in a dynamic language (without overloading)?
- How can you manipulate your grammar to simplify your JTB-based visitors?
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