

## Solution

### Series 03 — 02.10.2019 – v1.0

## Safety & Synchronization

### Exercise 1 (2 Points)

Answer the following questions:

- a) What does a safety property do in FSP and how do you model it? **Answer:**

*A safety property  $P$  consists of (textual or mathematical) definitions describing properties of a model. These definitions can be implemented within a deterministic process. This process asserts that any trace with actions in the alphabet of  $P$ , is accepted by  $P$  (i.e. not violating any safety constraints). It is possible to define a safety property using the keyword “property” and defining the legal action trace that the model has to follow.<sup>1</sup> The tool then creates an additional error state (-1) during the evaluation of the model which receives all the invalid transitions from each state (i.e., which would lead to an error state).*

- b) Is the busy-wait mutex protocol fair? Justify your answer. **Answer:**

*This protocol is fair because a process always gives priority to the other process to enter the critical section. So they, in theory, can alternately enter in the critical section. Moreover, it has been formally proven to be deadlock free (see the FSP in the lecture).*

- c) Can you ensure safety in concurrent programs without using any kind of locks? **Answer:**

*No, to ensure safety you need some sort of locks, because you have to guarantee that only one thread at a time can access shared resources. The sole case where you don't need locks is, obviously, when there is no shared mutable state.*

- d) The Java language designers decided to implement concurrency based on monitors. What is the main reason behind this decision? What other options except monitors could have been chosen?

*Hint: Consider page number 40 of the intro lecture (01) PDF available online. **Answer:***

*The notion of monitors is similar to the notion of objects. The concepts of semaphores and message passing could also be used for ensuring safety and liveness, but because of their complex configurations these are not that easily adaptable to existing language specifications. For example, imagine the Java language designers relied on semaphores instead of monitors. Accordingly, you would have to provide every time an additional number specifying the amount of concurrent threads that are allowed in the critical section, when you use the synchronized keyword.*

### Exercise 2 (1 point)

Consider the following FSP process definitions. Are T1 and T2 equivalent? Why?

$$\begin{aligned} R &= (a \rightarrow c \rightarrow R) . \\ S &= (b \rightarrow c \rightarrow S) . \\ || T1 &= (R || S) . \\ T2 &= (a \rightarrow b \rightarrow c \rightarrow T2 | b \rightarrow a \rightarrow c \rightarrow T2) . \end{aligned}$$

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<sup>1</sup>You can find an example in section 1.8 at [https://www.doc.ic.ac.uk/ltsa/eclipse/help/index.html?appendix\\_b\\_\\_\\_fsp\\_language\\_spec.htm](https://www.doc.ic.ac.uk/ltsa/eclipse/help/index.html?appendix_b___fsp_language_spec.htm)

**Answer:**

Yes, because the only possible action traces are “a, b, c” and “b, a, c” for both processes.

**Exercise 3 (3 points)**

A miniature portable FM radio has three controls. An on/off switch turns the device on and off. Frequency tuning is controlled by two buttons, scan and reset, which operate as follows: When the radio is turned on or reset is pressed, the radio is tuned to the top frequency of the FM frequency band. When scan is pressed, the radio scans towards the bottom of the band. It stops scanning when it locks on a station or it reaches the bottom end. If the radio is currently tuned to a station and scan is pressed then it starts to scan from the frequency of that station downwards. Similarly, when reset is pressed the receiver tunes to the top.

Use the alphabet {on, off, scan, reset, lock, end} to model the FM radio as an FSP process called RADIO and generate the corresponding LTS using the LTSA tool. **Answer:**

```
RADIO = OFF,  
OFF = (on-> TOP),  
BOTTOM = (off -> OFF | scan -> SCANNING | reset -> TOP),  
TOP = (off -> OFF | scan -> SCANNING | reset -> TOP),  
SCANNING = (off -> OFF | lock -> LOCKED | end -> BOTTOM | reset -> TOP),  
LOCKED = (off -> OFF | scan -> SCANNING | reset -> TOP).
```

**Exercise 4 (4 points)**

Implement a stack in LTS and obey the following requirements:

- a) There exists one PUSH process which provides the push functionality.
- b) There exists one POP process that provides the pop functionality.
- c) There exists one LOCK process that provides the locking functionality.
- d) There exists one STACK process that provides the stack functionality.
- e) The stack has two slots to store values.
- f) The stack operations *pop* and *push* must use a lock (each acquiring the lock before and releasing it after the push/pop operation).
- g) The supported data values are only 0 and 1 (*i.e.*, you can only *push* 0s and 1s).
- h) An error must be thrown for *pushing* to a full stack or *popping* from an empty stack.

You can verify your model using the LTSA tool.

*Hint: Try to first model the processes PUSH, POP, and LOCK on paper. After that you can assemble the STACK process by reusing them properly. You should not try to build only one process for the whole stack, because the result would be super complex. Instead, you can use the "COMPOSE" feature of the FSP tool which does that for you automatically.*

**Answer:**

*In the solution below, we modeled stack errors as actions (i.e., transitions). Another, although less favorable approach, would be to represent stack errors with a common explicit “error state”.*

```
range BIT = 0..1

LOCK = ( lock -> unlock -> LOCK ).

STACK = S0,
S0 = ( push[v:BIT] -> ok -> S1[v]
      | pop[u:BIT] -> error -> S0 ),
S1[v:BIT] = ( pop[v] -> ok -> S0
             | push[u:BIT] -> ok -> S2[v][u] ),
S2[v:BIT][u:BIT] = ( pop[u] -> ok -> S1[v]
                    | push[x:BIT] -> error -> S2[v][u] ).

set Ops = { pop[BIT], push[BIT], error, ok }

PUSH = ( lock -> push[v:BIT] ->
         ( ok -> unlock -> PUSH
         | error -> unlock -> PUSH ) ) +Ops.

POP = ( lock -> pop[v:BIT]->
        ( ok -> unlock -> POP
        | error -> unlock -> POP ) ) +Ops.

||Stack2 = ({a,b}::STACK || a:PUSH || b:POP || {a,b}::LOCK) .
```