

6. Intermediate Representation

Oscar Nierstrasz

Thanks to Jens Palsberg and Tony Hosking for their kind permission to reuse and adapt the CS132 and CS502 lecture notes.
<http://www.cs.ucla.edu/~palsberg/>
<http://www.cs.purdue.edu/homes/hosking/>

SSA lecture notes by Marcus Denker

Roadmap

- > Intermediate representations
- > Static Single Assignment
- > SSA generation
- > Dominance and SSA generation
- > Applications of SSA
- > Φ -congruence and SSA removal



See, *Modern compiler implementation in Java* (Second edition), chapters 7-8.

Roadmap

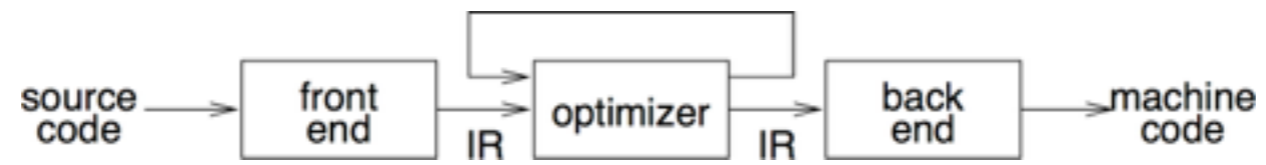


- > **Intermediate representations**
- > Static Single Assignment
- > SSA generation
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Why use intermediate representations?

1. **Software engineering principle**
 - break compiler into manageable pieces
2. **Simplifies retargeting to new host**
 - isolates back end from front end
3. **Simplifies support for multiple languages**
 - different languages can share IR and back end
4. **Enables machine-independent optimization**
 - general techniques, multiple passes

IR scheme



- front end produces IR
- optimizer transforms IR to more efficient program
- back end transforms IR to target code

Kinds of IR

- > Abstract syntax trees (AST)
- > Linear operator form of tree (e.g., postfix notation)
- > Directed acyclic graphs (DAG)
- > Control flow graphs (CFG)
- > Program dependence graphs (PDG)
- > Static single assignment form (SSA)
- > 3-address code
- > Hybrid combinations

Categories of IR

> Structural

- graphically oriented (trees, DAGs)
- nodes and edges tend to be large
- heavily used on source-to-source translators

> Linear

- pseudo-code for abstract machine
- large variation in level of abstraction
- simple, compact data structures
- easier to rearrange

> Hybrid

- combination of graphs and linear code (e.g. CFGs)
- attempt to achieve best of both worlds

Important IR properties

- > Ease of generation
- > Ease of manipulation
- > Cost of manipulation
- > Level of abstraction
- > Freedom of expression (!)
- > Size of typical procedure
- > Original or derivative

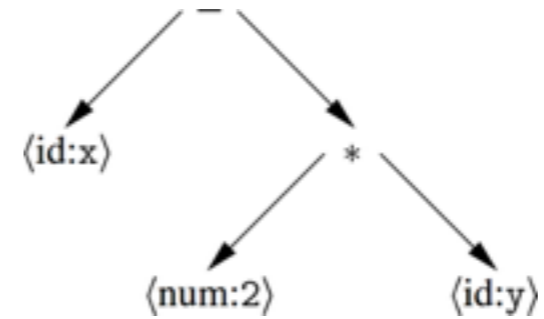
Subtle design decisions in the IR can have far-reaching effects on the speed and effectiveness of the compiler!

→ *Degree of exposed detail can be crucial*

Abstract syntax tree

An AST is a parse tree with nodes for most non-terminals removed.

Since the program is already parsed, non-terminals needed to establish precedence and associativity can be collapsed!



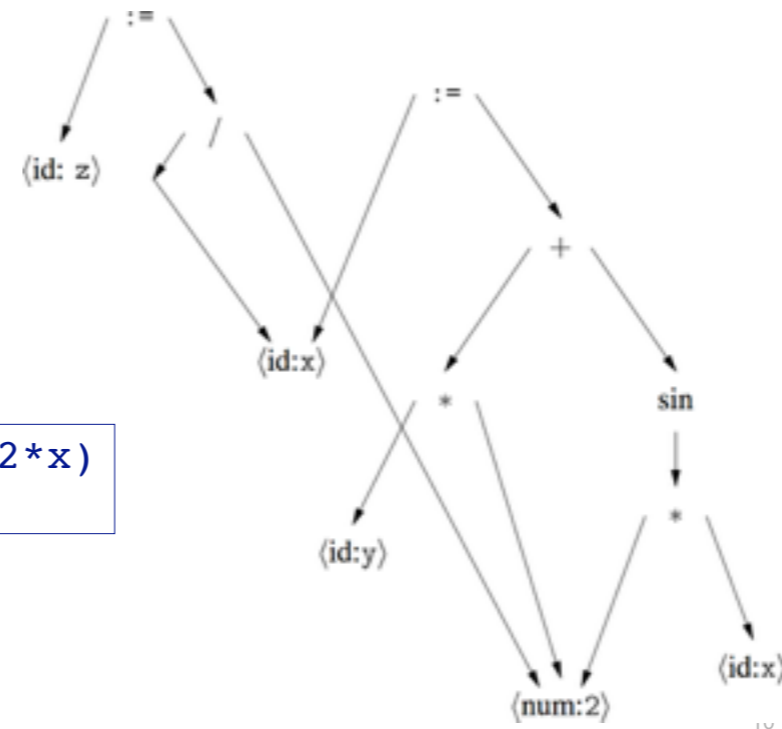
A linear operator form of this tree (postfix) would be:

x 2 y * -

Directed acyclic graph

A DAG is an AST with unique, shared nodes for each value.

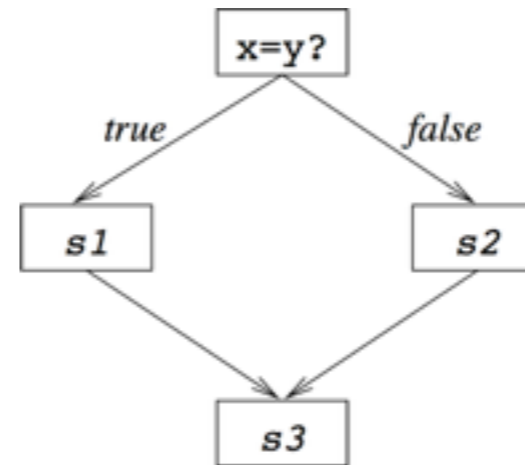
```
x := 2 * y + sin(2*x)
z := x / 2
```



Control flow graph

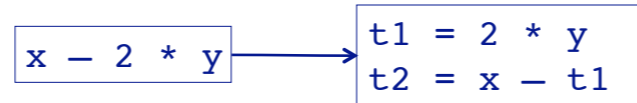
- > A CFG models *transfer of control* in a program
 - nodes are *basic blocks* (straight-line blocks of code)
 - edges represent *control flow* (loops, if/else, goto ...)

```
if x = y then
  S1
else
  S2
end
S3
```



3-address code

- > Statements take the form: $x = y \text{ op } z$
 - single operator and at most three names



- > Advantages:
 - compact form
 - names for intermediate values

Typical 3-address codes

<i>assignments</i>	<code>x = y op z</code>
	<code>x = op y</code>
	<code>x = y[i]</code>
	<code>x = y</code>
<i>branches</i>	<code>goto L</code>
<i>conditional branches</i>	<code>if x relop y goto L</code>
<i>procedure calls</i>	<code>param x</code> <code>param y</code> <code>call p</code>
<i>address and pointer assignments</i>	<code>x = &y</code> <code>*y = z</code>

3-address code — two variants

Quadruples

$x - 2 * y$				
(1)	load	t1	y	
(2)	loadi	t2	2	
(3)	mult	t3	t2	t1
(4)	load	t4	x	
(5)	sub	t5	t4	t3

- simple record structure
- easy to reorder
- explicit names

Triples

$x - 2 * y$			
(1)	load	y	
(2)	loadi	2	
(3)	mult	(1)	(2)
(4)	load	x	
(5)	sub	(4)	(3)

- table index is implicit name
- only 3 fields
- harder to reorder

IR choices

- > Other hybrids exist
 - combinations of graphs and linear codes
 - CFG with 3-address code for basic blocks
- > Many variants used in practice
 - no widespread agreement
 - compilers may need several different IRs!
- > Advice:
 - choose IR with right level of detail
 - keep manipulation costs in mind

Roadmap



- > Intermediate representations
- > **Static Single Assignment**
- > SSA generation
- > Dominance and SSA generation
- > Applications of SSA
- > Φ -congruence and SSA removal

SSA: Literature

Books:

- SSA Chapter in Appel
- Chapter 8.11 Muchnik



SSA Creation:

Cytron et. al: *Efficiently computing Static Single Assignment Form and the Control Dependency Graph* (TOPLAS, Oct 1991)

Φ -**Removal**: Sreedhar et al. *Translating out of Static Single Assignment Form* (SAS, 1999)

Static Single Assignment Form

> Goal: simplify procedure-global optimizations

> *Definition:*

Program is in SSA form if every variable
is only assigned once

Static Single Assignment (SSA)

- > Each assignment to a temporary is given a unique name
 - All uses reached by that assignment are renamed
 - Compact representation
 - Useful for many kinds of compiler optimization ...

<pre>x := 3; x := x + 1; x := 7; x := x*2;</pre>	➔	<pre>x₁ := 3; x₂ := x₁ + 1; x₃ := 7; x₄ := x₃*2;</pre>
--	---	--

Ron Cytron, et al., "Efficiently computing static single assignment form and the control dependence graph," ACM TOPLAS., 1991. doi:10.1145/115372.115320

http://en.wikipedia.org/wiki/Static_single_assignment_form

Why *Static*?

- > Why *Static*?
 - *We only look at the static program*
 - *One assignment per variable in the program*
- > At runtime variables are assigned multiple times!

Example: Sequence

Easy to do for sequential programs:

Original

```
a := b + c
b := c + 1
d := b + c
a := a + 1
e := a + b
```

SSA

```
a1 := b1 + c1
b2 := c1 + 1
d1 := b2 + c1
a2 := a1 + 1
e1 := a2 + b2
```

SSA form makes clear that a₂ is not the same as a₁, so easier for analysis

Example: Condition

Conditions: what to do on control-flow merge?

Original

```
if B then
  a := b
else
  a := c
end
... a ...
```

SSA

```
if B then
  a1 := b
else
  a2 := c
end
... a? ...
```

is it a1 or is it a2?

Solution: Φ -Function

Conditions: what to do on control-flow merge?

Original

```
if B then
  a := b
else
  a := c
end
... a ...
```

SSA

```
if B then
  a1 := b
else
  a2 := c
end
a3 :=  $\Phi(a_1, a_2)$ 
... a3 ...
```

is it a1 or is it a2?

The Φ -Function

- > Φ -functions are always at the beginning of a basic block
- > Selects between values depending on control-flow
- > $a_{k+1} := \Phi(a_1 \dots a_k)$: the block has k preceding blocks

Φ -functions are evaluated simultaneously within a basic block.

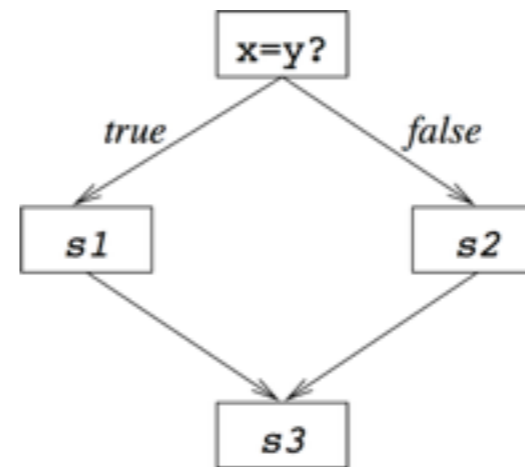
SSA and CFG

- > SSA is normally used for control-flow graphs (CFG)
- > Basic blocks are in 3-address form

Recall: Control flow graph

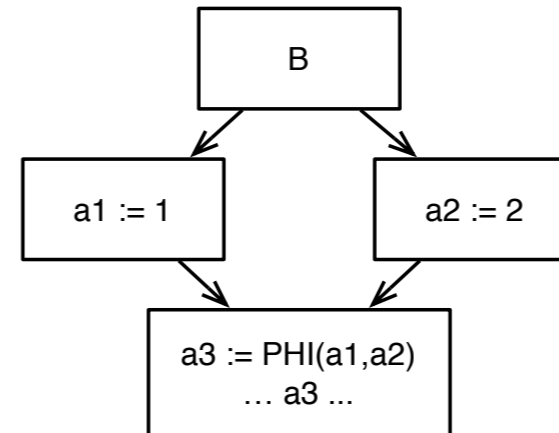
- > A CFG models *transfer of control* in a program
 - nodes are *basic blocks* (straight-line blocks of code)
 - edges represent *control flow* (loops, if/else, goto ...)

```
if x = y then
  S1
else
  S2
end
S3
```



SSA: a Simple Example

```
if B then
  a1 := 1
else
  a2 := 2
end
a3 :=  $\Phi(a1, a2)$ 
... a3 ...
```

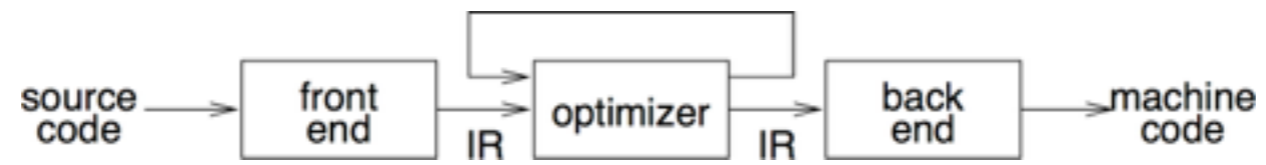


Roadmap



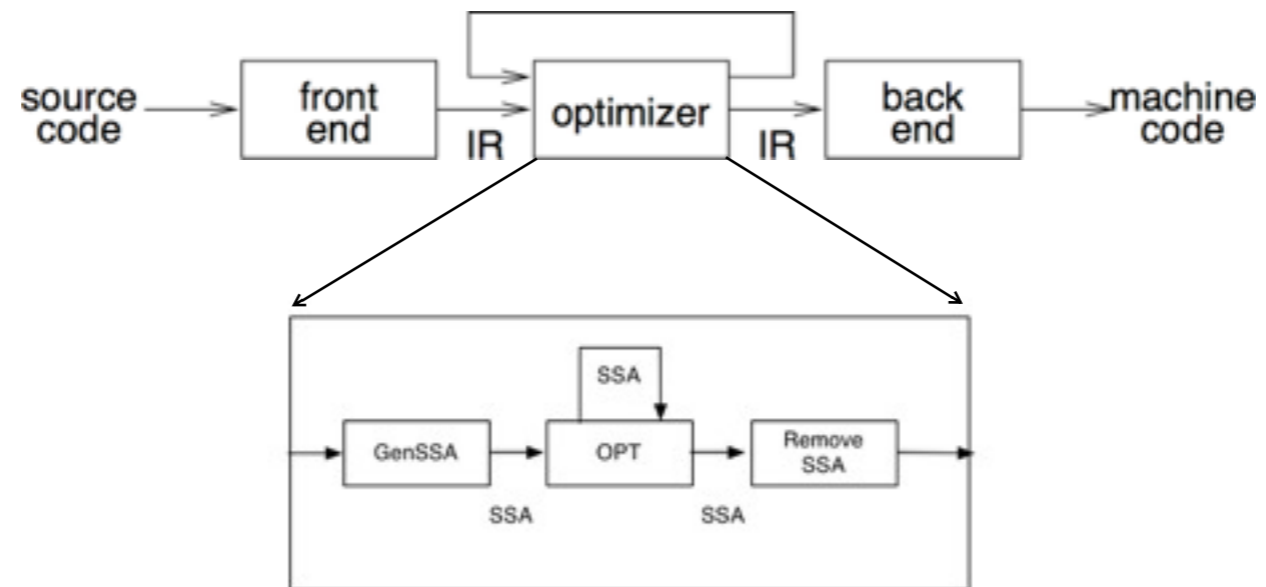
- > Intermediate representations
- > Static Single Assignment
- > **SSA generation**
- > Dominance and SSA generation
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Recall: IR



- front end produces IR
- optimizer transforms IR to more efficient program
- back end transform IR to target code

SSA as IR



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Current trend in compiler community is to use SSA as *the* IR for everything in back end.
(NB: for compilers that generate machine code, not those that generate bytecode.)

Transforming to SSA

- > ***Problem: Performance / Memory***

- Minimize number of inserted Φ -functions
- Do not spend too much time

- > ***Many relatively complex algorithms***

- We do not go too much into detail
- See literature!

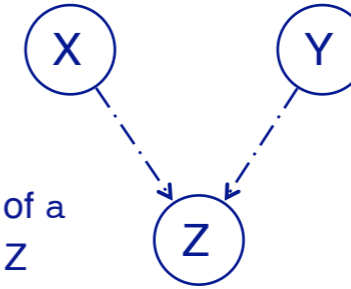
Minimal SSA

- > Two steps:
 - Place Φ -functions
 - Rename Variables
- > Where to place Φ -functions?
- > We want minimal amount of needed Φ
 - Save memory*
 - Algorithms will work faster*

Path Convergence Criterion

> There should be a Φ for a at node Z if:

1. There is a block X containing a definition of a
2. There is a block Y ($Y \neq X$) containing a definition of a
3. There is a nonempty path P_{xz} of edges from X to Z
4. There is a nonempty path P_{yz} of edges from Y to Z
5. Path P_{xz} and P_{yz} do not have any nodes in common other than Z
6. The node Z does not appear within both P_{xz} and P_{yz} prior to the end (although it may appear in one or the other)



> *I.e., Z is the first place where two definitions of a collide*

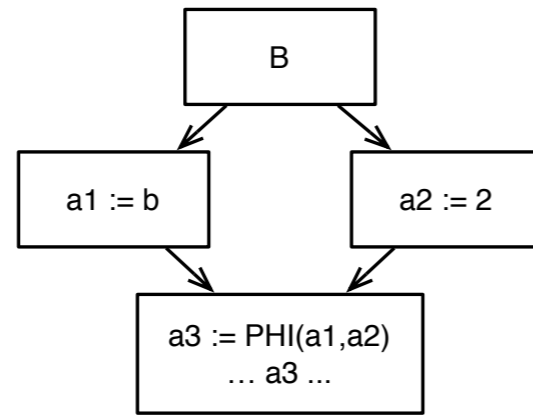
Iterated Path-Convergence

> Inserted Φ is itself a definition!

```
while there are nodes X,Y,Z satisfying conditions 1-5  
  and Z does not contain a  $\Phi$ -function for a  
  do  
    insert  $\Phi$  at node Z.
```

*A bit slow, other algorithms
used in practice*

Example (Simple)



1. block X contains a definition of a
2. block Y ($Y \neq X$) contains a definition of a
3. path P_{xz} of edges from X to Z.
4. path P_{yz} of edges from Y to Z.
5. path P_{xz} and P_{yz} do not have any nodes in common other than Z
6. node Z does not appear within both P_{xz} and P_{yz} prior to the end

Roadmap



- > Intermediate representations
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- > **Dominance and SSA generation**
- > Applications of SSA
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Dominance Property of SSA

- > Dominance: node D *dominates* node N if every path from the start node to N goes through D .
("strictly dominates": $D \neq N$)

Dominance Property of SSA:

1. If x is used in a Φ -function in block N , then the node defining x dominates every predecessor of N .
2. If x is used in a non- Φ statement in N , then the node defining x dominates N

"Definition dominates use"

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NB: If x is used in a Φ -function in N , then there is another path to N , but not to its predecessors.

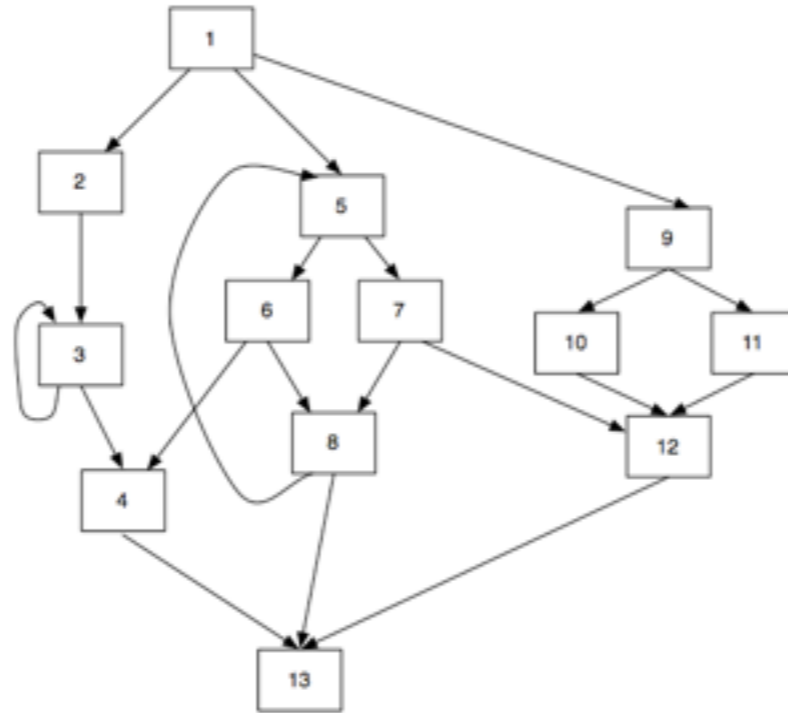
Dominance is a property of basic blocks. (one Node dominates a set of nodes).

For the dominance property, "definition of x " thus means the basic block in which x is defined.

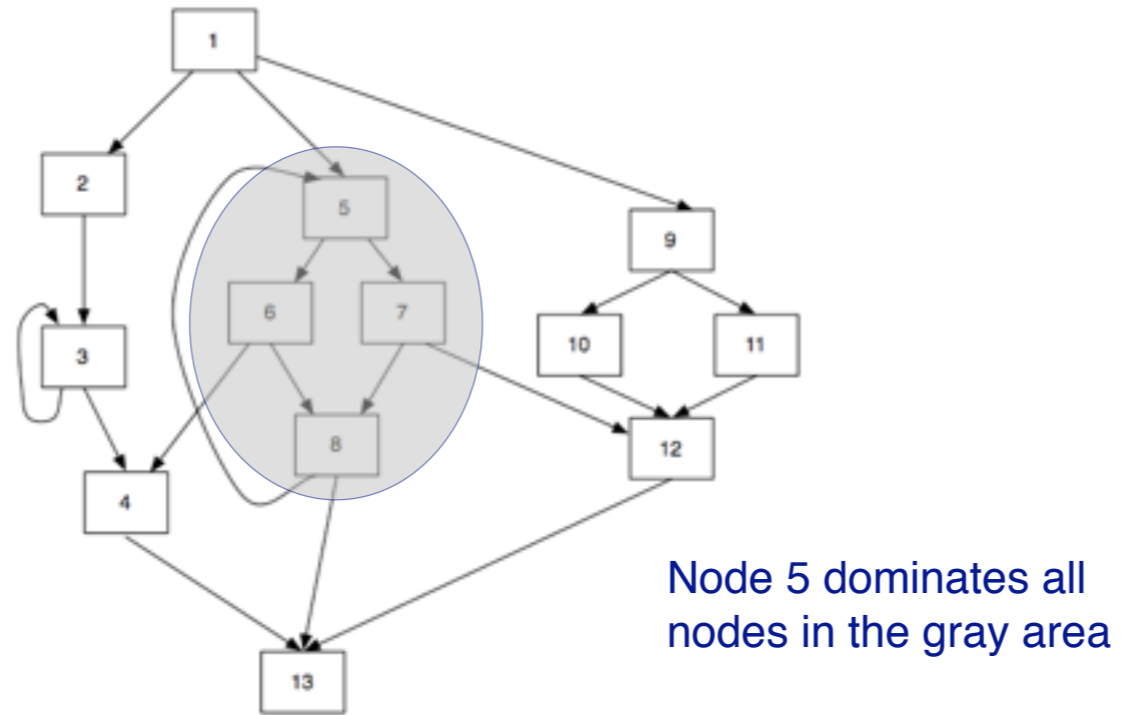
Dominance and SSA Creation

- > Dominance can be used to efficiently build SSA
- > Φ -Functions are placed in all basic blocks of the *Dominance Frontier*
 - DF(D) = the set of all nodes N such that D dominates an immediate predecessor of N but does not strictly dominate N.

Dominance frontier



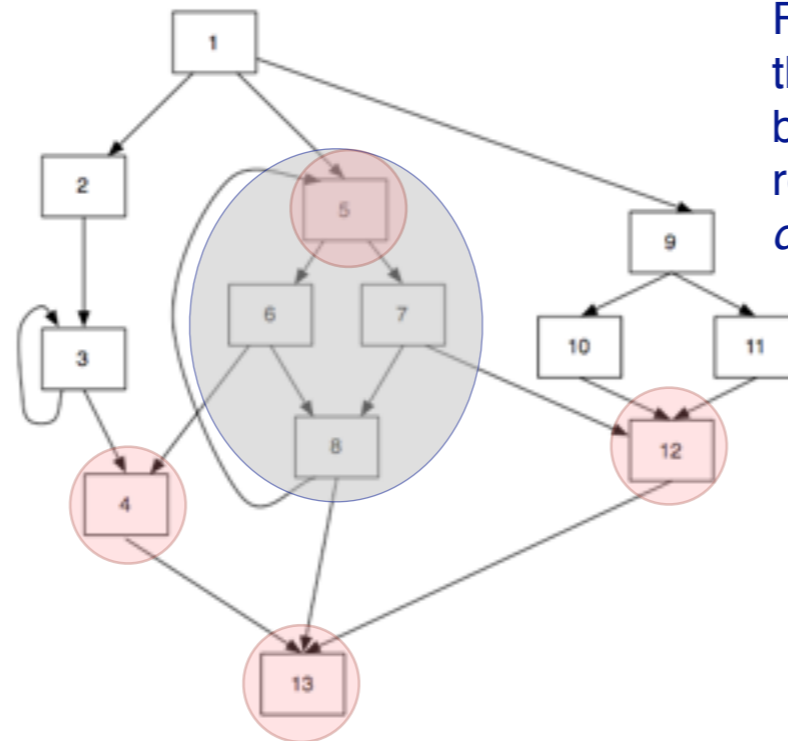
Dominance frontier



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I.e., there is no path to any of these nodes except through node 5.

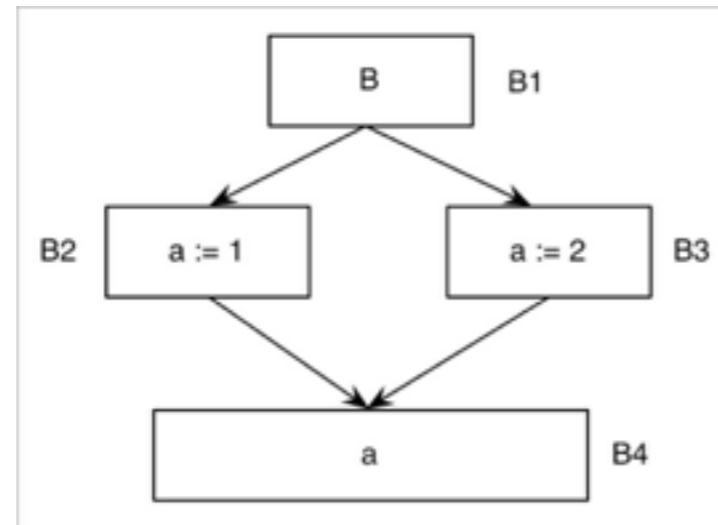
Dominance frontier



Follow edges leaving the region dominated by node 5 to the region not *strictly dominated* by 5.

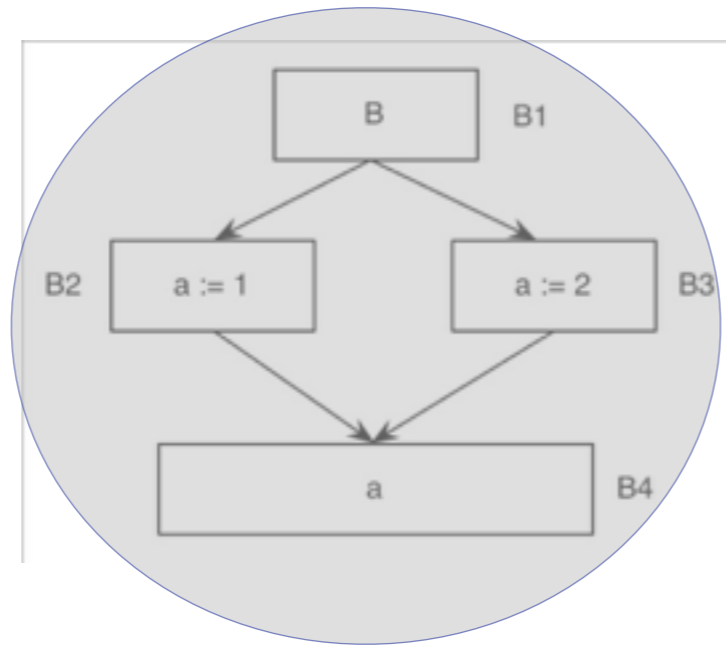
$DF(5) = \{4, 5, 12, 13\}$

Simple Example



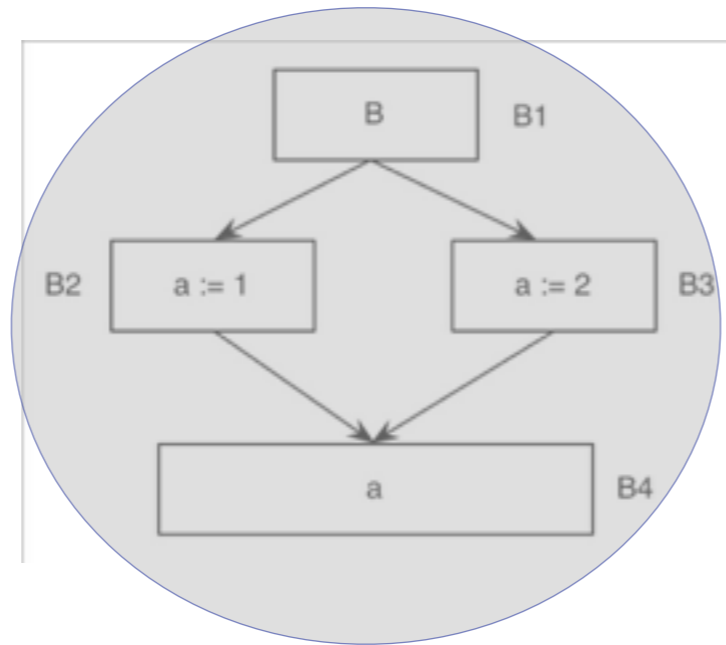
DF(B1)=
DF(B2)=
DF(B3)=
DF(B4)=

Simple Example



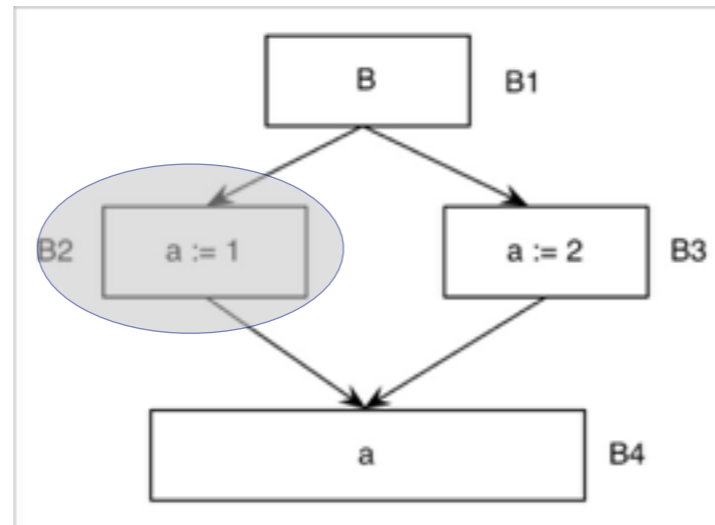
DF(B1)={?}
DF(B2)=
DF(B3)=
DF(B4)=

Simple Example



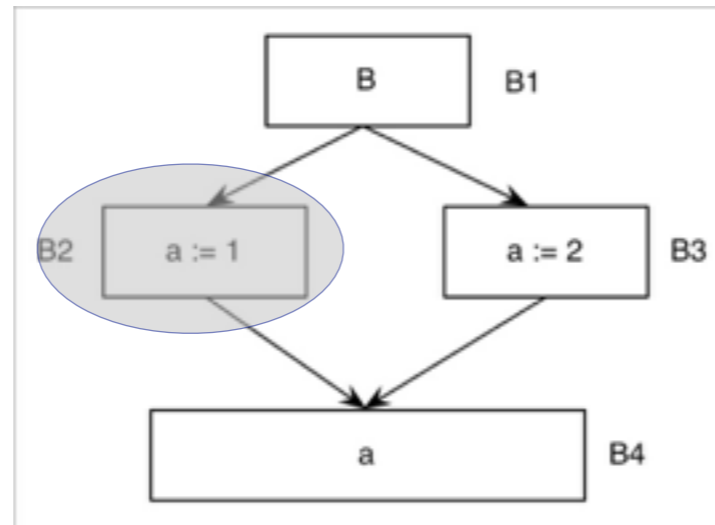
$DF(B1)=\{\}$
 $DF(B2)=$
 $DF(B3)=$
 $DF(B4)=$

Simple Example



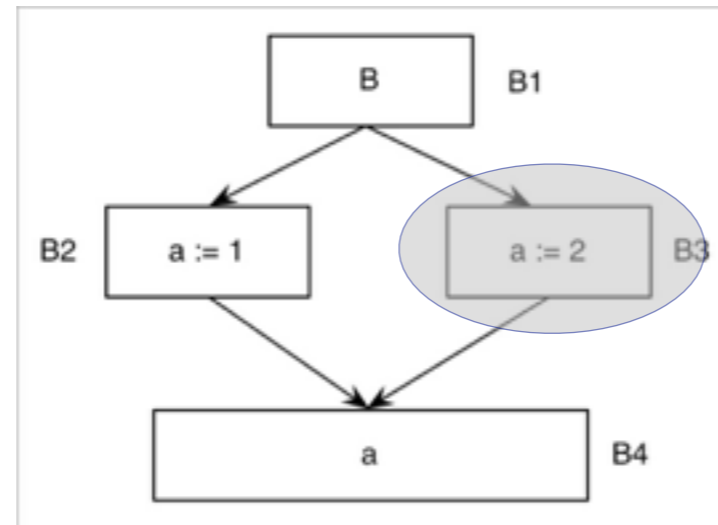
DF(B1)={}
DF(B2)={?}
DF(B3)=
DF(B4)=

Simple Example



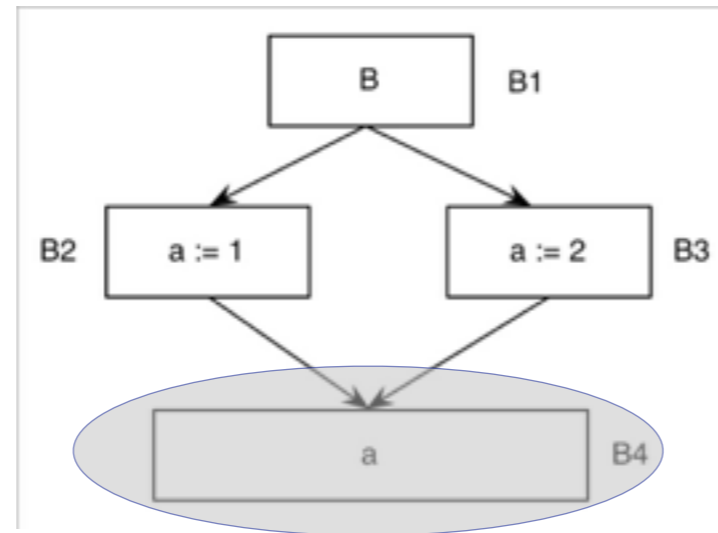
$DF(B1) = \{\}$
 $DF(B2) = \{B4\}$
 $DF(B3) =$
 $DF(B4) =$

Simple Example



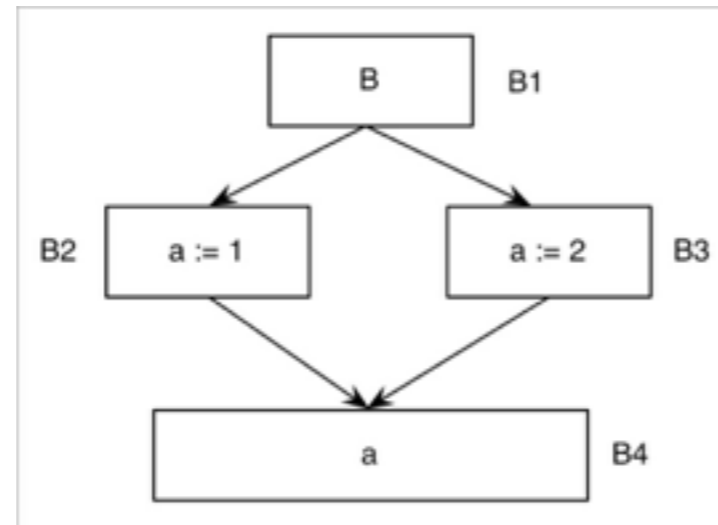
$DF(B1) = \{\}$
 $DF(B2) = \{B4\}$
 $DF(B3) = \{B4\}$
 $DF(B4) =$

Simple Example



$DF(B1)=\{\}$
 $DF(B2)=\{B4\}$
 $DF(B3)=\{B4\}$
 $DF(B4)=\{\}$

Simple Example



$DF(B1)=\{\}$
 $DF(B2)=\{B4\}$
 $DF(B3)=\{B4\}$
 $DF(B4)=\{\}$

Φ -Function needed in B4 (for a)

Roadmap



- > Intermediate representations
- > Static Single Assignment
- > SSA generation
- > Dominance and SSA generation
- > **Applications of SSA**
- > Φ -congruence and SSA removal

Properties of SSA

> Simplifies many optimizations

- *Every variable has only one definition*
- *Every use knows its definition, every definition knows its uses*
- *Unrelated variables get different names*

> Examples:

- *Constant propagation*
- *Value numbering*
- *Invariant code motion and removal*
- *Strength reduction*
- *Partial redundancy elimination*

Next lecture!

Constant propagation: substitute constants and evaluate constant expressions

Value numbering: number values & expressions to eliminate redundant computation

Invariant code motion and removal: move invariant code out of loops

Strength reduction: replace expensive operations by equivalent, cheaper ones (eg multiplication by addition)

Partial redundancy elimination: move common subexpressions to eliminate recomputation

SSA in the Real World

- > Invented end of the 80s, a lot of research in the 90s
- > Used in many modern compilers
 - *ETH Oberon 2*
 - *LLVM*
 - *GNU GCC 4*
 - *IBM Jikes Java VM*
 - *Java Hotspot VM*
 - *Mono*
 - *Many more...*

Roadmap



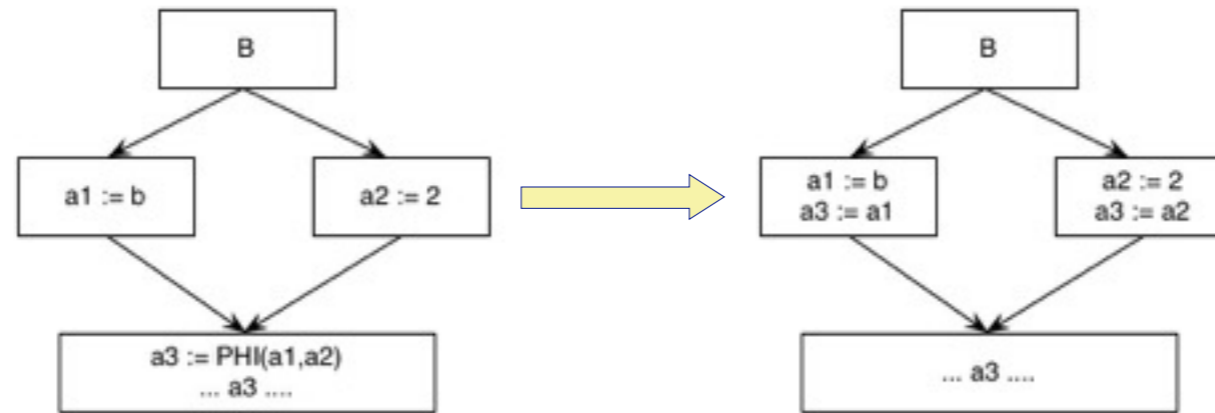
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Vugranam C. Sreedhar, et al, "Translating Out of Static Single Assignment Form", LNCS 1694, 1999, doi:10.1007/3-540-48294-6_13

Transforming out-of SSA

- > Processor cannot execute Φ -Function
- > How do we remove it?

Simple Copy Placement



Naive copy placement may produce incorrect results after optimization ...

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Here we simply push the assignments to a3 up to each branch.
Sreedhar shows that the naive approach can be wrong if variables “interfere”.

Φ -Congruence

Idea: transform program so that all variables in Φ are the same:

$a1 = \Phi(a1, a1)$  $a1 = a1$

- > Insert Copies
- > Rename Variables

Φ -Congruence: Definitions

Φ -connected(x):

$$a3 = \Phi(a1, a2)$$

$$a5 = \Phi(a3, a4)$$

$a1, a2, a3$ are Φ -connected

$a3, a4, a5$ are Φ -connected

Φ -congruence-class:

Transitive closure of Φ -connected(x).

$a1$ - $a5$ are Φ -congruent

x and y are connected if they are used or defined in the same Φ instruction

Φ -Congruence Property

Φ -congruence property:

All variables of the same congruence class can be replaced by one representative variable without changing the semantics.

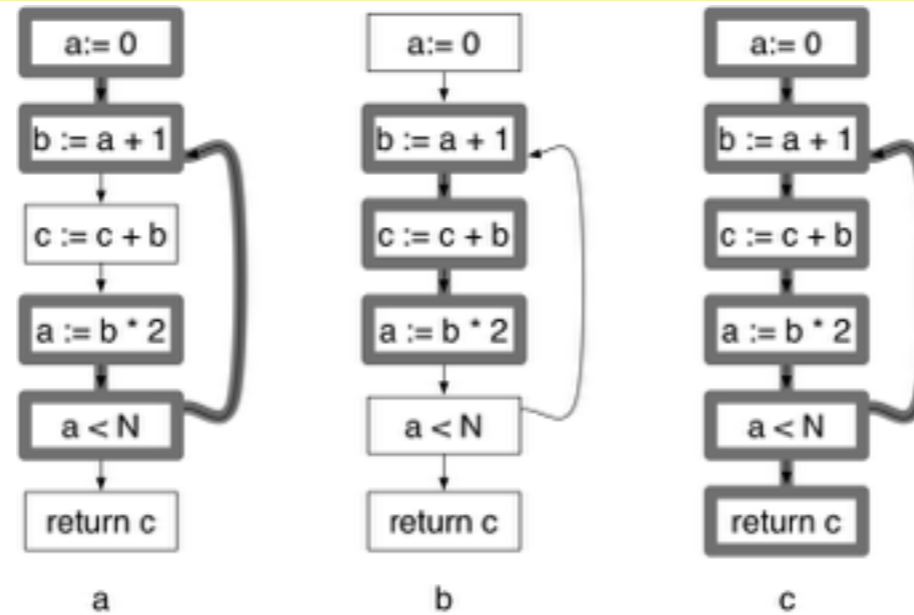
SSA without optimizations has Φ -congruence property

Variables of the congruence class never live at the same time (by construction)

The property obviously holds before optimization, since all Φ -connected variables started out as the same variable.

Liveness

A variable v is *live* on edge e if there is a path through e to a use of v not passing through an assignment to v

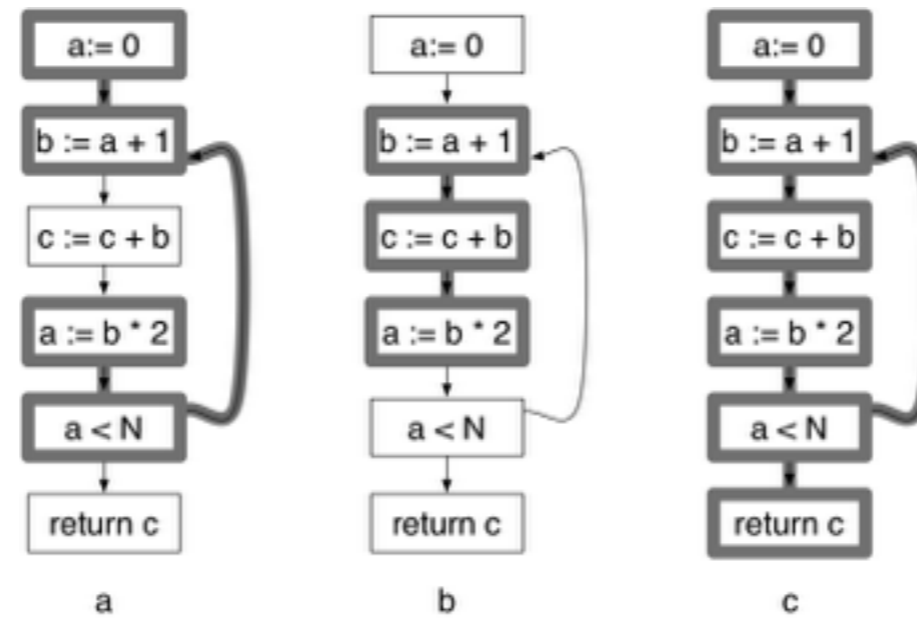


a and b are never live on the same edges, so two registers suffice to hold a, b and c

I.e., follow paths from assignments to last use before a new assignment.

NB: c is implicitly assigned when it is defined, so is live from the start to its first use.

Interference



a and c are live at the same time: interference

Φ -Removal: Big picture

- > CSSA: SSA with Φ -congruence-property.
 - *directly after SSA generation*
 - *no interference*

 - > TSSA: SSA without Φ -congruence-property.
 - *after optimizations*
 - *Interference*
1. Transform TSSA into CSSA (fix interference)
 2. Rename Φ -variables
 3. Delete Φ

CSSA = Conventional SSA
TSSA = Transformed SSA

SSA and Register Allocation

- > Idea: remove Φ as late as possible
- > Variables in Φ -function never live at the same time!
 - *Can be stored in the same register*
- > Do register allocation on SSA!

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So, don't remove Φ functions before register allocation! Keep them till end.
(Many reasons to keep SSA as IR for various phases in the back end.)

What you should know!

- ✎ Why do most compilers need an intermediate representation for programs?*
- ✎ What are the key tradeoffs between structural and linear IRs?*
- ✎ What is a “basic block”?*
- ✎ What are common strategies for representing case statements?*
- ✎ When a program has SSA form.*
- ✎ What is a Φ -function.*
- ✎ When do we place Φ -functions*
- ✎ How to remove Φ -functions*

Can you answer these questions?

- ✎ Why can't a parser directly produced high quality executable code?*
- ✎ What criteria should drive your choice of an IR?*
- ✎ What kind of IR does JTB generate?*
- ✎ Why can we not directly generate executable code from SSA?*
- ✎ Why do we use 3-address code and CFG for SSA?*



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